

**SEMESTER STUDY PLAN**  
**INTRODUCTION TO MEASURE THEORY AND LEBESGUE**  
**INTEGRAL**  
**(ELECTIVE COURSE)**



**DEPARTMENT OF MATHEMATICS AND DATA SCIENCE**  
**FACULTY OF MATHEMATICS AND NATURAL SCIENCES**  
**UNIVERSITAS ANDALAS**  
**2024**



**SEMESTER STUDY PLAN (SSP)**  
**BACHELOR PROGRAM OF MATHEMATICS**  
**FACULTY OF MATHEMATICS AND NATURAL SCIENCES**  
**UNIVERSITAS ANDALAS**

Course Name		Course Code	URL I-Learn	Credits	Semester	Compilation Date
Introduction to Measure Theory and Lebesgue Integral		MAT62222	<a href="https://sci.ilearn.unand.ac.id">https://sci.ilearn.unand.ac.id</a>	3	6	11 May 2024
Person In Charge		Study Plan Creator		Head of Research Group		Head of Study Program
		Dr. Shelvi Ekariani		Dr. Haripamyu		Dr. Noverina Alfiany
Intended Learning Outcomes (ILO) and Performance Indicator (PI)	Intended Learning Outcomes					
	ILO-2	Possesses profound knowledge of the basic concept mathematics PI-1: An ability to explain basic mathematical concepts PI-2: An ability to provide examples that are relevant to basic mathematical concepts PI-3: An ability to determine solutions to simple problems using basic mathematical concepts				
	ILO-3	An ability to identify, explain and generalize simple mathematical PI-1: An ability to identify simple mathematical problems PI-2: An ability to explain simple mathematical problems PI-3: An ability to generalize simple mathematical problems				
	ILO-4	An ability to use concept and fundamental technique of mathematics in solving simple mathematical problems PI-1: An ability to choose appropriate basic mathematical concepts and techniques in solving simple mathematical problems PI-2: An ability to illustrate simple mathematical problems based on appropriate basic mathematical concepts and techniques PI-3: An ability to solve simple mathematical problems using appropriate basic mathematical concepts and techniques				

	<b>ILO-5</b>	<p>An ability to formally and correctly proves a simple mathematical statements using facts and methods that have been studied</p> <p>PI-1: An ability to identify the formal structures and analogous forms in mathematics</p> <p>PI-2: An ability to use facts and apply methods to prove simple mathematical statements</p> <p>PI-3: An ability to present simple mathematical statement proof rigorously (sequentially and conscientious)</p> <p>PI-4: An ability to conclude or interpret result of the proving simple mathematical statement</p>
	<b>ILO-9</b>	<p>An ability to apply knowledge of mathematics in career and involve in lifelong learning</p> <p>PI-1: An ability to carry out learning independently to deepen and expand the knowledge that has been obtained</p>
	<b>Course Learning Outcomes</b>	
	1	An ability to mastery the basic concepts of measure and Lebesgue integral, as well as their related properties. ( <b>ILO-2:</b> PI-1, PI-2, PI-3)
	2	An ability to apply the basic properties learned to solve problems related to the course material. ( <b>ILO-4:</b> PI-1, PI-2, PI-3)
	3	An ability to generalize problems related to the subject matter of this course. ( <b>ILO-3:</b> PI-1, PI-2, PI-3)
	4	An ability to identify the formal structure of statements related to the course material and their analogous forms. ( <b>ILO-5:</b> PI-1-4)
	5	An ability to mastery of fundamental techniques necessary for problem-solving within the scope of this course material. ( <b>ILO-4:</b> PI-1, PI-2, PI-3)
	6	An ability to independently solve problems related to the theory of measure and Lebesgue integral. ( <b>ILO-9:</b> PI-1)

<b>Brief Description</b>	This course provides experience for students to know about sigma algebras, measures, outer measures, measurable spaces, measure spaces, measurable sets and functions, simple functions, Lebesgue integral, and $L^p$ spaces.	
<b>Course Materials</b>	Sigma Algebra, Measurable Space, Measure, Measure Space, Outer Measure, Measurable Set, Measurable Function, Simple Function, Equivalence Relation, Lebesgue Integral, $L^p$ Space.	
<b>References</b>	<b>Main:</b>	1. D. L. Cohn. (2013). <i>Measure Theory</i> . 2 <sup>nd</sup> edition. Springer, New York
	<b>Additional:</b>	2. J. K. Hunter. (2011). <i>Measure Theory</i> . Lectures Note
<b>Learning Media</b>	<b>Software:</b>	<b>Hardware:</b>
	<ul style="list-style-type: none"> <li>• LMS Unand (<a href="http://fmipa.ilearn.unand.ac.id/">http://fmipa.ilearn.unand.ac.id/</a>)</li> <li>• Zoom meeting</li> <li>• Whatsapp</li> </ul>	<ul style="list-style-type: none"> <li>• Computer/Laptop</li> <li>• Smartphone</li> </ul>
<b>Team Teaching</b>	Dr. Shelvi Ekariani	
<b>Assessment</b>	Homework, Quizzes, Mid-Term exam, Final exam	
<b>Required courses</b>	Real Analysis 1	
<b>Academic Norms</b>	<a href="https://akademik.unand.ac.id/images/2022-03-30%20Peraturan%20Rektor%20Nomor%207%20Tahun%202022%20Penyelenggaraan%20Pendidikan-khusus%20Bab%20II.pdf">https://akademik.unand.ac.id/images/2022-03-30%20Peraturan%20Rektor%20Nomor%207%20Tahun%202022%20Penyelenggaraan%20Pendidikan-khusus%20Bab%20II.pdf</a>	

## Weekly Study Plan

Week / Meet (1)	Course Outcomes (2)	Indicator (3)	Assessment (4)	Activities/Forms of Learning [Time estimated]					Subject, references (10)	Weight (11)
				Synchronous*		Asynchronous**		Media (9)		
				Face to face Offline (5)	Face to face Online (6)	Individual (7)	Collaboration (8)			
1	CLO-1 An ability to mastery the basic concepts of measure and Lebesgue integral, as well as their related properties. (ILO-2: PI-1, PI-2, PI-3)	<ul style="list-style-type: none"><li>Discipline in carrying out the course contract.</li><li>Accuracy in understanding related material.</li></ul>	Non test  Test Mid-Term exam: 10% Quizzes 1: 3%	Teaching and discussion:  <ul style="list-style-type: none"><li>Explanation of Semester Learning Plan</li><li>explanation of learning material</li><li>explanation of the task</li><li>explanation of the assessment</li></ul> [1 × 3 × 50 minutes]	Teaching and discussion:  <ul style="list-style-type: none"><li>Explanation of Semester Learning Plan</li><li>explanation of learning material</li><li>explanation of the task</li><li>explanation of the assessment</li></ul> [1 × 3 × 50 minutes]  (Specific conditions: The total number of blended learning	Students read and study learning materials related to real number systems and their properties  [1 × 3 × 120 minutes]		<ul style="list-style-type: none"><li>PPT</li><li>I learn (LMS Unand)</li><li>(Specific condition: Zoom meeting, WA group, learning video)</li></ul>	<ul style="list-style-type: none"><li>Course Introduction</li><li>Description course</li></ul> References:  Main Reference 1.	13%

					meetings is 40% of the total number of meetings)					
2	CLO-3 An ability to generalize problems related to the subject matter of this course. (ILO-3: PI-1, PI-2, PI-3)	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	Non test Test Mid-Term exam: 3% Quizzes 1: 3%	Lectures and discussions  [1 × 3 × 50 minutes]		Students read and study materials from the main reference and others. [1 × 3 × 120 minutes]		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Sigma Algebra</li> <li>• Examples of Sigma Algebras</li> </ul> <p>Reference: Main Reference 1.</p>	3%
3	CLO-2 An ability to apply the basic properties learned to solve problems related to the course material. (ILO-4: PI-1, PI-2, PI-3)	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> </ul>	Non test: Homework 1: 3% Test Mid-Term exam: 5%	Lectures and discussions  [1 × 3 × 50 minutes]		Students read and study materials from the main reference and others. [1 × 3 × 120 minutes]		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting,</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Measurable Space</li> <li>• Examples of Measurable Spaces</li> </ul>	8%

		<ul style="list-style-type: none"> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>						WA group, learning video)	Reference: Main Reference 1.	
4-5	<p>CLO-1 An ability to mastery the basic concepts of measure and Lebesgue integral, as well as their related properties. (ILO-2: PI-1, PI-2, PI-3)</p> <p>CLO-6 An ability to independently solve problems related to the theory of measure and Lebesgue integral. (ILO-9: PI-1)</p>	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	<p>Non test : -</p> <p>Test: Mid-Term exam: 10% Quizzes 1: 2%</p>	<p>Lectures and discussions</p> <p>[1 × 3 × 50 minutes]</p>		<p>Students read and study materials from the main reference and others</p> <p>[1 × 3 × 120 minutes]</p>		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Measure</li> <li>• Examples of Measures</li> <li>• Definition of Measure Space</li> <li>• Examples of Measure Spaces</li> </ul> <p>Reference: Main Reference 1.</p>	12%
6-7	<p>CLO-2 An ability to apply the basic properties learned to solve</p>	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> </ul>	<p>Non test: Homework 1: 2%</p>	<p>Lectures and discussions</p>		<p>Students read and study materials from the main</p>		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Outer Measure</li> </ul>	11%

	<p>problems related to the course material. (<b>ILO-4:</b> PI-1, PI-2, PI-3)</p> <p>CLO-3 An ability to generalize problems related to the subject matter of this course. (<b>ILO-3:</b> PI-1, PI-2, PI-3)</p>	<ul style="list-style-type: none"> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	<p>Test Mid-Term exam: 7% Quizzes 1: 2%</p>	<p>[1 × 3 × 50 minutes]</p>		<p>reference and others</p> <p>[1 × 3 × 120 minutes]</p>		<ul style="list-style-type: none"> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Examples of Outer Measures</li> <li>• Definition of Measurable Set</li> <li>• Examples of Measurable Sets</li> </ul> <p>Reference: Main Reference 1.</p>	
8	<b>MID-TERM EXAM</b>									
9-10	<p>CLO-3 An ability to generalize problems related to the subject matter of this course. (<b>ILO-3:</b> PI-1, PI-2, PI-3)</p> <p>CLO-4 An ability to identify the formal structure of statements related to the course material</p>	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	<p>Non test : Test Final exam: 12% Quizzes 2: 1%</p>	<p>Lectures and discussions</p> <p>[2 × 3 × 50 minutes]</p>		<p>Students read and study materials from the main reference and others</p> <p>[2 × 3 × 120 minutes]</p>		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Measurable Function</li> <li>• Examples of Measurable Functions</li> <li>• Definition of Characteristic Function</li> <li>• Properties of</li> </ul>	<b>13%</b>

	and their analogous forms. (ILO-5: PI-1-4)								Characteristic Functions  Reference: Main Reference 1.	
11-13	<p>CLO-4 An ability to identify the formal structure of statements related to the course material and their analogous forms. (ILO-5: PI-1-4)</p> <p>CLO-5 An ability to mastery of fundamental techniques necessary for problem-solving within the scope of this course material. (ILO-4: PI-1, PI-2, PI-3)</p> <p>CLO-6 Ability to independently solve problems related to the theory of</p>	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	<p>Non test: Homework 2: 5%</p> <p>Test Final exam: 15% Quizzes 2: 7%</p>	<p>Lectures and discussions</p> <p>[2 × 3 × 50 minutes]</p>		<p>Students read and study materials from the main reference and others</p> <p>[2 × 3 × 120 minutes]</p>		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Definition of Simple Function</li> <li>• Canonical Representation</li> <li>• Examples of Simple Functions</li> <li>• Equivalence Relation</li> <li>• Equivalence Class</li> <li>• Examples of Equivalence Relations and Equivalence Classes</li> </ul>	27%

	measure and Lebesgue integral. (ILO-9: PI-1)									
14-15	<p>CLO-2 Ability to apply the basic properties learned to solve problems related to the course material. (ILO-4: PI-1, PI-2, PI-3)</p> <p>CLO-4 Ability to identifying the formal structure of statements related to the course material and their analogous forms. (ILO-5: PI-1-4)</p> <p>CLO-6 Ability to independently solve problems related to the theory of measure and Lebesgue</p>	<ul style="list-style-type: none"> <li>• Accuracy in understanding related material</li> <li>• Accuracy in answering assignment questions</li> <li>• Neatness in completing assignments</li> <li>• Originality of assignment results</li> </ul>	<p>Non test:</p> <p>Test</p> <p>Final exam: 8%</p> <p>Quizzes 2: 2%</p>	<p>Lectures and discussions</p> <p>[2 × 3 × 50 minutes]</p>		<p>Students read and study materials from the main reference and others</p> <p>[2 × 3 × 120 minutes]</p>		<ul style="list-style-type: none"> <li>• PPT</li> <li>• I learn (LMS Unand)</li> <li>• (Specific condition: Zoom meeting, WA group, learning video)</li> </ul>	<ul style="list-style-type: none"> <li>• Lebesgue Integral</li> <li>• Examples of Lebesgue Integrable Functions</li> <li>• <math>L^p</math> Space</li> <li>• Properties of <math>L^p</math> Spaces</li> </ul>	10%

	integral. (ILO-9: PI-1)									
Total Weight										100%
16	FINAL EXAM									

1 credit = 50 minutes face-to-face meeting, 60 minutes structured study, 60 minutes independent study  
Each meeting duration is 3 credits = 3×50 minutes

### Indicators, Criteria, and Assessment Weights

#### 1. Assessment weight for each Assessment

NO	Assessment	Weight (%)
1	Mid-Term Exam	35
2	Final Exam	35
3	Homework	10
4	Quizzes	20
<b>TOTAL</b>		<b>100</b>

#### 2. Assessment weight for Intended Learning Outcome

- CLO-1: 20 %
- CLO-2: 20 %
- CLO-3: 20 %
- CLO-4: 10 %
- CLO-5: 20 %
- CLO-6: 10%

**Assessment Plan Table:**

No.	CLO	Assessment				Weight (%)
		Homework (%)	Quizzes (%)	Mid-Term Exam (%)	Final Exam (%)	
1	An ability to mastery the basic concepts of measure and Lebesgue integral, as well as their related properties. (ILO-2: PI-1, PI-2, PI-3)		Quizzes 1: 5	15		20
2	An ability to apply the basic properties learned to solve problems related to the course material. (ILO-4: PI-1, PI-2, PI-3)	Homework 1: 5		10	5	20
3	An ability to generalize problems related to the subject matter of this course. (ILO-3: PI-1, PI-2, PI-3)		Quizzes 1: 5	5	10	20

4	An ability to identify the formal structure of statements related to the course material and their analogous forms. ( <b>ILO-5</b> : PI-1-4)		Quizzes 2: 5		5	10
5	An ability to mastery of fundamental techniques necessary for problem-solving within the scope of this course material. ( <b>ILO-4</b> : PI-1, PI-2, PI-3)	Homework 2: 5	Quizzes 2: 5		10	20
6	An ability to independently solve problems related to the theory of measure and Lebesgue integral. ( <b>ILO-9</b> : PI-1)			5	5	10
<b>Total</b>		<b>10</b>	<b>20</b>	<b>35</b>	<b>35</b>	<b>100</b>

# Matrix of CLO and ILO

CLO	ILO																															
	1			2			3			4			5				6					7			8				9			
	PI			PI			PI			PI			PI				PI					PI			PI				PI			
	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3	4	1	2	3	4	5	1	2	3	1	2	3	4	1	2	3	4
1				□	□	□																										
2										□	□	□																				
3							□	□	□																							
4													□	□	□	□																
5										□	□	□																				
6																													□			

